RMAC – A LIGHTWEIGHT AUTHENTICATION PROTOCOL FOR HIGHLY CONSTRAINED IOT DEVICES

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ABSTRACT

Nowadays, highly constrained IoT devices have earned an important place in our everyday lives. These devices mainly comprise RFID (Radio-Frequency Identification) or WSN (Wireless Sensor Networks) components. Their adoption is growing in areas where data security or privacy or both must be guaranteed. Therefore, it is necessary to develop appropriate security solutions for these systems. Many papers have proposed solutions for encryption or authentication. But it turns out that sometimes the proposal has security flaw or is ill-suited for the constrained IoT devices (which has very limited processing and storage capacities). In this paper, we introduce a new authentication protocol inspired by Mirror-Mac (MM) which is a generic construction of authentication protocol proposed by Mol et al. Our proposal named RMAC is well suited for highly constrained IoT devices since its implementation uses simple and lightweight algorithms. We also prove that RMAC is at least as secure as the MM protocol and thus secure against man-in-the-middle attacks.

KEYWORDS

IoT, MAC, authentication, lightweight protocol, Xor-Cascade Encryption

1. INTRODUCTION

The Internet of Things (IoT), refers to a wide variety of devices that can collect, share data and more to connect to the internet. These devices mainly comprise RFID or WSN components [1]. Data security and privacy constitute one of the biggest issues with the IoT since extremely sensitive data can be collected and shared anonymously [1]. Therefore, in order to maintain the growing interest (and trust) in connected objects in healthcare, in the retail supply chain and in the automotive industry to name a few, security in their implementation must be taken into account. Unfortunately, classical cryptographic primitives require important processing and storage capacities that constrained IoT devices do not have [2]. Therefore, it is necessary to invent secure and lightweight solutions. But designing such lightweight protocols is not easy, since they must take into account security, hardware efficiency and energy consumption. Nevertheless, several solutions for lightweight authentication protocol have been proposed. We can mention HB-like protocols [3–5], Message Authentication Codes [6–8] exploiting the difficulty of the LPN problem and others [2,9–14].

In this paper, we propose a new 3-round MAC authentication protocol named RMAC (stands for Random MAC). One might ask why a new lightweight authentication protocol since there is a bunch of proposals. The answer is simply because many of the aforementioned proposals have been broken [15–20] or have a storage and transmission cost unacceptably high [4,6] for highly constrained IoT devices. This new protocol is inspired by the MM proposal [21], i.e. a 2-round authentication protocol based on weak MACs and provably secure against man-in-the-middle attacks. It also exploits the well-studied $r$-round Xor-Cascade Encryption, i.e. a framework for designing block ciphers.

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The main idea behind the MM proposal is that the prover responds to the verifier only if the pair $(M, \tau_1)$ received is correct (see figure 1). Since the used MAC is unforgettable under random-message attack (uf-rma), any modification of the pair $(M, \tau_1)$ stops the execution of the protocol. Therefore, the attacker has very little chance to have any information about the keys used in the authentication protocol. But the weakness of this method is that the attacker can use an isolated prover as a verification oracle because he can send a pair $(M, \tau_1)$ to the prover and if the latter responds he will know that the pair is good and at the same time he will have for free $TAG_{\mathcal{K}_2}(M)$ for any M of his choice. The RMAC protocol that we propose here eliminates this shortcoming.

The $r$-round Xor-Cascade Encryption is a framework for designing block ciphers from random permutations [22–25]. RMAC implements a 2-round Xor-Cascade Encryption as a message authentication code. We know that the 2-round Xor-Cascade Encryption is secure up to $2^{k+n/2}$ query complexity [22]. That is an adversary cannot gain useful information about the key with less than $2^{k+n/2}$ queries to both the 2-round Xor-Cascade Encryption itself and to its inner permutations. But this threshold can be easily reached when the attacker has at his disposal a genuine prover. Therefore, in order to overcome this weakness, we execute a key establishment protocol before the core authentication protocol to renew the key at each authentication session.

This paper is structured as follows. A brief introduction is done in section 1 followed by some definitions in section 2. Section 3 presents existing work. Our RMAC protocol is described in section 4 followed by the security arguments that weighs in its favor in section 5. Finally, a conclusion is given in section 6.

2. Definition

2.1. r-round Xor-Cascade Encryption

The $r$-round Xor-Cascade Encryption (which can also be seen as a Generalized Even-Mansour\(^1\) Cipher) can be considered as a framework for building block ciphers from a set of random permutations. Consider an ensemble \(\mathcal{P} = \{P_i\}_{i \in [0,1]}\) of random permutations of \(\{0,1\}^n\), the $r$-round Xor-Cascade Encryption $\mathcal{XC}_r^P$ with $r \leq 2^k$ defines a block cipher with message space $\{0,1\}^n$ and key space $\{0,1\}^{(r+1)n+k\tau}$ as follow: given a key $(k, w)$ where $k = (k_0, k_1, \ldots, k_r) \in \{(0,1)^n\}^{r+1}$, $w = (i_0, i_1, \ldots, i_r) \in \{(0,1)^n\}^{r}$, and a message $x \in \{0,1\}^n$,

\[
\mathcal{XC}_r^P(k, w, x) = k_r \oplus P_{i_r}(k_{r-1} \oplus P_{i_{r-1}}(\cdots P_{i_1}(k_1 \oplus P_{i_1}(k_0 \oplus x)) \cdots ))
\] (1)

A considerable number of papers [22–25] have shown that, in the model where the adversary is given oracle access to inner permutations $P_i \in \mathcal{P}$ of her choice and their inverses and to the outer permutation $\mathcal{XC}_r^P$, the security of the $r$-round Xor-Cascade Encryption approaches $2^{k+n}$ when $r$ is increasing. Also, other papers explored attacks on these constructions [27–30].

2.2. Message Authentication Codes

A message authentication code (MAC) is a triple of probabilistic polynomial-time algorithms $(KGEN, TAG, VRFY)$ such that:

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\(^1\)The Generalized Even-Mansour Cipher is a generalization of the one-round Even-Mansour schema [26].
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1. **KGEN** is the key generation algorithm. It takes as input a security parameter $1^n$ and outputs a key $K$ from a specified key space $\mathcal{K}$.

2. **TAG** is the MAC tag generation algorithm (may be randomized). It takes as input a key $K$ and a message $M$ from a specified message space $\mathcal{M}$ and outputs a MAC tag $\tau \leftarrow TAG_K(M)$.

3. **VRFY** is the verification algorithm (assumed to be deterministic). It takes as input a key $K$, a message $M$ and a MAC tag $\tau$ and outputs a bit $b = VRFY(M, \tau)$. If the TAG algorithm is a cipher as in our RMAC protocol, $VRFY$ outputs 1 if $\tau = TAG_K(M)$ or 0 otherwise.

The security of a MAC is related to its resistance against forgery. The strongest notion of MAC security is suf-cma, that is strongly unforgettable under chosen-message attack. It refers to MACs for which any adversary has negligible chance to generate a valid MAC tag for a new message (a message whose MAC tag is not previously seen by the adversary) even if she has seen MAC tags for messages of its choosing. Our RMAC protocol is based on a weaker MAC (uf-rma MAC) that is a MAC which is unforgettable only under random-message attack. That is, the MAC is unforgettable if the adversary does not have the ability to perform chosen-message attack. The adversary can only see MAC tags for random messages (messages for which she has no control).

### 2.3. MITM secure authentication protocol

Man-in-the-middle (MITM) attacks are the most powerful attacks against authentication protocols [6]. The MITM adversary is allowed to interact several times (at will and even concurrently) with the prover and the verifier. An authentication protocol achieves MITM security if any MITM adversary cannot bring the verifier to accept.

### 3. Existing Work

A number of works has been done on lightweight authentication protocols. There is HB-like protocols [3–5] which take advantage of the difficulty of solving the learning parity with noise (LPN) problem. The probabilistic nature of the verifier’s final response (accepting or rejecting the prover) in HB-like protocols is generally exploited to develop attacks against them [17–19]. In addition, despite their attractive design, which implies low computing resource requirements, their communication cost is often very high. Thus, it is hard to see an efficient HB-like protocol secure against man-in-the-middle attacks. However, there are other lightweight authentication protocols based on MACs. For example, SQUASH [2] based on the Rabin encryption scheme, and others based on the LPN problem [6, 7, 31]. The proposals of Kiltz et al. [6] are MAC-based authentication protocols exploiting the difficulty of the LPN problem. These protocols have the advantage of having a tight reduction to the LPN problem and therefore secure against man-in-the-middle attacks. But they suffer from the large size of their keys and their large communication complexity. All these drawbacks make these protocols poorly suited for highly constrained IoT devices. More recent proposals have been made [9–12] but it turns out that [9, 10] fail to achieve the claimed security level [15, 16].

The proposal of Mol et al. named Mirror-Mac (MM) [21] has caught our attention. MM is a generic construction of a 2-round MITM secure protocol (see figure 1). Mol et al. have proven that when instantiated with an uf-rma (unforgettable under random-message attack) MAC, MM is secure even if the adversary interacts at will with an arbitrary number of both prover and verifier instances. That is the adversary has negligible chance to make the verifier to accept. Our proposal RMAC is inspired by MM.
Figure 1: The generic MM construction of a 2-round MITM secure protocol proposed by Mol et al. [21]. Using MAC = (KGEN, TAG, VRFY) where the keys $K_1$ and $K_2$ are generated by KGEN, TAG takes as input a key $K$ and a message $M$ in a message space $\mathcal{M}$ and outputs $\text{TAG}_K(M)$ and VRFY takes as input a key $K$, a message $M$ and a MAC tag $\tau$ in the tag space $\mathcal{T}$ then outputs a decision $\text{VRFY}_K(M, \tau) \in \{0,1\}$.

4. THE NEW PROTOCOL

Traditionally, a MAC authentication is a 2 steps protocol. The verifier and the prover share a common secret $K$. The verifier sends a challenge $M$ to the prover that calculates and returns the corresponding tag $\tau \leftarrow \text{TAG}_K(M)$ to the verifier. The latter checks if the received tag is correct $\text{VRFY}_K(M, \tau) = 1$ to accept the prover. For such a scheme to be secure it is necessary that the MAC be suf-cma since the adversary has a direct access to it and can make chosen-message attacks. Such MACs are generally constructed from traditional pseudorandom functions unusable in a highly constrained environment because they require heavy computation. A solution for highly constrained IoT devices is to use a MAC consisting of lightweight algorithms (certainly less sure than conventional MACs) and embed it in a protocol from which the adversary will not have a direct access to make chosen-message attacks. Therefore, the adversary is forced to be passive. It’s that solution that we implement with our protocol.

RMAC is an authentication protocol that uses a 128-bit key and operates with 64-bit challenge and 64-bit response. In the rest of the paper, we set $n = 64$. RMAC is based on the two-round generic construction of an in-the-middle secure authentication protocol denoted MM introduced by Mol et al. [21]. But in our protocol the challenge is encrypted using a one-time pad prior to sending it to the prover and whatever the result of the verification of the pair $(\text{pfx}_n(\beta), \tau_1)$ by the prover an $n$-bit string is returned to the verifier (see figures 1 and 2 for a graphical comparison of MM and RMAC).

Figure 2: The RMAC authentication protocol using SC with keys $K_1, K_2, S_1$ and $\text{pfx}_n(\beta)$ is the prefix of length $n$ of $\beta$. 
The RMAC protocol also uses a new implementation of a Xor-Cascade Encryption consisting of only two rounds as an uf-rma message authentication code. Using this small number of rounds guaranties low-latency and low-cost hardware implementation [32]. In the rest of this paper, we call Small-Cipher or SC that implementation of the 2-round Xor-Cascade Encryption. We know from [22] that the 2-round Xor-Cascade Encryption is secure up to \(2^{k+n/2}\) query complexity. When such construction is implemented in highly constrained devices (this must be a lightweight implementation) with a fixed key, the security threshold of \(2^{k+n/2}\) queries can be easily reached. Thus, in order to make such an attack difficult and burdensome, we renew the key with a lightweight key establishment protocol.

4.1. The Lightweight Key Establishment Protocol

The lightweight key establishment protocol we describe here is run before the core authentication protocol. Figure 2 shows how the key establishment protocol works. The two parties share a secret key \(S\) of size \(2n\). The prover begins by drawing uniformly at random \(\alpha\) from \(\{0,1\}^{2n}\) and then sends it to the verifier. They both compute \(S' = \text{MixBits}(S, \alpha)\) where MixBits is a mixing function. After that, the verifier draws uniformly at random \(\beta\) from \((0,1)^{2n}\), computes \(\beta' = \beta \oplus S'\) and sends the result to the prover. Finally the two parties derive two \(n\)-bit long secret keys \(K_1\) and \(K_2\) by using \(\Delta(\beta, S')\). The function \(\Delta\) acts as a comb on \(\beta\) with \(n\) teeth randomly spaced, the space between the teeth is defined by \(S'\) (see algorithm 1). Any secure lightweight mixing function can be used but here we propose to use the mixing function introduced in the Gossamer protocol because it has an extremely lightweight nature [14] (see below).

The MixBits function:

\[
Z = \text{MixBits}(X, Y) \\
Z = X; \\
\text{for}(i=0; i<32; i++) \\
\quad Z = (Z>>1) + Z + Z + Y ;
\]

Algorithm 1: \(\Delta(X, S)\). Deriving two bit strings \(K_1\) and \(K_2\) from \(X\) using \(S\) as a comb.

Input: Two \(2n\)-bit strings \(X = x_1...x_{2n}\) and \(S = s_1...s_{2n}\)

Output: Two \(n\)-bit strings \(K_1\) and \(K_2\)

Processing:

1. Initialize \(K_1 \leftarrow \text{null}\)
2. Initialize \(K_2 \leftarrow \text{null}\)
3. Initialize \(b \leftarrow 0\)
4. if \(\text{wt}(S) > n\) then \(b \leftarrow 1\)
5. for \(i = 1...2n\) do
6. if \(s_i = b\) and \(|K_1| < n\) then
7. \(K_1 \leftarrow K_1 || s_i\)
8. else \(K_2 \leftarrow K_2 || s_i\)

4.2. Design Details of the Core Authentication Protocol

The prover and the verifier share a long-lived key \(S\) and two session keys \(K_1\) and \(K_2\) obtained from the lightweight key establishment protocol. The verifier draws a random \(2n\)-bit string \(\beta\), computes \(\beta' = \beta \oplus S'\) and \(\tau_4 = \text{SC}(\text{pfx}_n(\beta))\) (where \(S'\) is computed during the session key establishment protocol, \(\text{pfx}_n(\beta)\) is the prefix of length \(n\) of \(\beta\)) then sends \((\beta', \tau_4)\) to the
prover. Upon receiving ($\beta'$, $\tau_1$), the prover checks whether $\tau_1$ is equal to $SC(pfx_n(\beta'))$, and if so, computes $\tau_2 = SC(\tau_1)$ and sends $\tau_2$ to the verifier. If not, it draws uniformly at random a $n$-bit string and sends it to the verifier. The latter accepts the prover if and only if $\tau_2 = SC(\tau_1)$.

Recall that $SC$ uses keys $K_1, K_2$ and $S$.

Now we present our Small-Cipher$^2$ (SC) which is an extremely lightweight implementation of the 2-roundXor-Cascade Encryption. It is used as a message authentication code (MAC) by RMAC. Its inner permutation is an SP-network denoted RBOX (stands for Random Box). Basically, an SP-network applies to its input (a plaintext and a key) many rounds of transformation each consisting of a random substitution of value of bits along the input text (using an S-box), a permutation of bit positions (using a P-box) and a key mixing. The P-boxes of SP-networks are usually a fixed permutation of the bit positions of state but here we introduce keyed one. In the rest of this section, we successively present the S-box, the P-box, RBOX (the Small-Cipher inner permutation) and Small-Cipher itself.

4.2.1. The S-box

It consists of a 4-bit to 4-bit S-box borrowed from the ultra-lightweight block cipher PRESENT [33]. This S-box is designed with hardware efficiency in mind for resource-limited devices. The following table recalls its action in hexadecimal notation.

<table>
<thead>
<tr>
<th>$x$</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>s-box[$x$]</td>
<td>C</td>
<td>5</td>
<td>6</td>
<td>B</td>
<td>9</td>
<td>0</td>
<td>A</td>
<td>D</td>
<td>3</td>
<td>E</td>
<td>F</td>
<td>8</td>
<td>4</td>
<td>7</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

4.2.2. The P-box

Let $L: \{0,1\}^n \times \{0,1\}^n \rightarrow \{0,1\}^n$ be the bit positions permutation we introduce here. That is for every $K \in \{0,1\}^n$, $L(K, \cdot)$ is a permutation on $\{0,1\}^n$ that preserves the hamming weight of its input. The way that $L_K(\cdot)$ computes the image of an input $X \in \{0,1\}^n$ is given by algorithm 2. For a randomly chosen $K \in \{0,1\}^n$, the first plot from the top of figure 3 shows how $L_K$ maps the original position of a bit of state to its new position. Note that the diffusion power of $L_K$ is weak because some streak of consecutive bits of state are not perturbed. We can also see from the plotting two groups of points forming two superimposed slopes. Bits of $K$, which are equal to 1, give the group at the top and bits of $K$, which are equal to 0, give the group at the bottom. In order, to achieve a better diffusion, we can iterate $L_K$ a number of times. Figure 3 shows the improvement obtained by iterating $L_K$.

Lemma 1 gives the relation that exists between the original position of a bit and its final position after $t$ iterations of $L_K$. Also, it becomes clear from lemma 1 that the more we iterate $L_K$ the more the final position of abit is unrelated to its original position but only depends on $K$.

---

$^2$It must be clear that SC is used as an uf-rma MAC for our authentication protocol and we do not claim to offer it as block cipher for constrained environments.
Algorithm 2: $L_k(X)$. Bit positions permutation.

**Input:** Two $n$-bit strings $K = k_1 \ldots k_n$ and $X = x_1 \ldots x_n$

**Output:** An $n$-bit strings $Y$

**Processing:**
1. Initialize $Y_0 \leftarrow \text{null}$
2. Initialize $Y_1 \leftarrow \text{null}$
3. for $i = 1 \ldots n$ do
   4. if $k_i = 0$ then
   5. \[ Y_0 \leftarrow Y_0 || x_i \]
   6. else $Y_1 \leftarrow Y_1 || x_i$
7. end
8. $Y \leftarrow Y_0 || Y_1$

---

**Figure 3:** Improvement of the diffusion power by iterating $L_k$, where $K$ is the 64-bit string $93E6748D4E52787C_{16}$. From top to bottom we have the 1st to the 5th iteration of $L_K$.

**4.2.3. The RBOX**

It is composed of the S-box presented earlier surrounded by two iterated P-Box layers. Since our P-boxes are keyed, let $K_1$ and $K_2$ be two $n$-bit keys, therefore RBOX$_{K_1K_2}$ consists of five iterations of $L_{K_1}$ followed by the S-box and five iterations of $L_{K_2}$ (see figure 4 for a depiction of RBOX$_{K_1K_2}$).

![Diagram of RBOX$_{K_1K_2}$]

**Figure 4:** RBOX$_{K_1K_2}$, the P-boxes $L_{K_1}$ and $L_{K_2}$ are iterated five times.
4.2.4. The Small-Cipher (SC)

In an initial phase, both the prover and the verifier hold the same 2n-bit secret key S. Let $S_1 = \text{prefix}_n(S)$ and $S_2 = \text{suffix}_n(S)$ be respectively the prefix of length $n$ of S and the suffix of length $n$ of S. From the execution of the lightweight key establishment protocol the two parties obtained two n-bit session keys $K_1$ and $K_2$. Since it is only required for the iterated Even-Mansour cipher to have the 3-round keys to be 2-wise independent [34]. Then, by using the two-independent n-bit permutations $\text{RBOX}_{K_1} S_1$ and $\text{RBOX}_{S_2 K_2}$ and the round keys $(K_1 \oplus K_2, K_2)$ we have our implementation of the 2-round Xor-Cascade Encryption depicted in Figure 5.

![Figure 5: Small-Cipher using keys $K_1, K_2, S_1$ and $S_2$](image)

A comparison of RMAC with other authentication protocols is given in table 1.

Table 1. Storage and transmission cost of some authentication protocols. Rabin crypto stands for Rabin cryptosystem, qSDH for q-Strong Diffie-Hellman, PUF for Physical Unclonable Function and 2-XC for 2-round Xor-Cascade Encryption. Values are given in bits.

<table>
<thead>
<tr>
<th>Protocol</th>
<th>Based on</th>
<th>Parameters</th>
<th>Key storage</th>
<th>Transmission cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>HB− [3]</td>
<td>LPN</td>
<td>$K_x = 80; K_y = 512$</td>
<td>592</td>
<td>690252</td>
</tr>
<tr>
<td>HB# [4]</td>
<td>LPN</td>
<td>$K_x = 80; K_y = 512; m = 1164$</td>
<td>2918</td>
<td>1756</td>
</tr>
<tr>
<td>SQUASH-128 [2]</td>
<td>Rabin crypto.</td>
<td>$(g, K) \in \mathbb{G} \times \mathbb{Z}_p$</td>
<td>?</td>
<td>$(M, \tau_1, \tau_2) \in \mathbb{Z}_p \times \mathbb{G}^2$</td>
</tr>
<tr>
<td>MM cryp. [21]</td>
<td>qSDH</td>
<td>$a = b = 16, m = 10, r = 6$</td>
<td>64</td>
<td>64</td>
</tr>
<tr>
<td>ETAP[11]</td>
<td>Dynamic Token</td>
<td>$a = b = 16, m = 10, r = 6$</td>
<td>64</td>
<td>64</td>
</tr>
<tr>
<td>H protocol[12]</td>
<td>PUF</td>
<td>$P_{\text{FID}} K_s$</td>
<td>288</td>
<td>576</td>
</tr>
<tr>
<td>RMAC</td>
<td>2-XC</td>
<td>S = 128</td>
<td>128</td>
<td>384</td>
</tr>
</tbody>
</table>

5. Security Arguments

In this section, we present the security analysis of SC and provide security proofs for RMAC.

5.1. Security of SC

5.1.1. The Structure of SC

SC is an implementation of the 2-round Xor-Cascade Encryption using RBOX as its inner permutation. The 2-round Xor-Cascade Encryption is secure up to $2^{k+n/2}$ query complexity [22]. For SC, $k = 2n$ thus SC is theoretically secure up to $2^{5n/2}$ queries to the underlying RBOXes and to SC itself. This bound is theoretical since the RBOXes cannot be considered as random permutations. This is why it is advantageous to change the RBOXes keys at each execution of RMAC. Also, note that through RMAC it is difficult for an adversary to make a chosen plaintext attack (and even more difficult a chosen ciphertext attack) against SC.
5.1.2. Resistance to Linear and Differential Cryptanalysis

Linear and differential cryptanalysis [35,36] are among the most famous tools used to analyse the security of a block cipher. But those cryptanalysis tools are heavily dependent on the S-boxes involved in the linear approximation or in the differential characteristic as we traverse the SP-network (the so-called active S-boxes). Theorem 1 implies that, using the iterated linear layer $L_K$ with a secret key $K$ makes complex to follow a bit of state through the SP-network. Therefore, it is very unlikely to determine the active S-boxes which are crucial to linear and differential cryptanalysis.

**Lemma 1.** Let $t \geq 0$ be an integer, $i$ be the position of a bit of state and $p^t(i)$ its position after $t$ iterations of $L_K$.

\[
p^t(i) = i - \sum_{r=0}^{t-1} (1 - k^r(i)) - \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t-1} (1 - k^u(i))
\]

Where $k^r(i)$ is the bit at position $p^r(i)$ of $K$, $w$ the Hamming weight of $K$ and $w^r(i)$ the Hamming weight of the prefix of length $p^r(i)$ of $K$.

**Proof.** We prove lemma 1 using the induction principle.

For $t = 0$ we have $p^0(i) = i$. Thus, equation 2 is true for $t = 0$.

Now we assume $t > 0$ and show that equation 2 holds for $t + 1$ iterations of $L_K$. From algorithm 1 we have:

\[
p(i) = \begin{cases} 
  i - w_i & \text{if } k_i = 0 \\
  n - w + w_i & \text{otherwise}
\end{cases}
\]

which leads to:

\[
p(i) = i(1 - k_i) + k_i(n - w + 2w_i) - w_i
\]

So

\[
p^{t+1}(i) = p^t(i)(1 - k^t(i)) + k^t(i)(n - w + 2w^t(i)) - w^t(i)
\]

By supposing that equation 2 is true, we have:

\[
p^{t+1}(i) = \left[ \prod_{r=0}^{t} (1 - k^r(i)) + \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t} (1 - k^u(i)) \right] (1 - k^t(i))
\]

\[
+ k^t(i)(n - w + 2w^t(i)) - w^t(i)
\]

\[
= i(1 - k^t(i)) \prod_{r=0}^{t} (1 - k^r(i)) + (1 - k^t(i)) \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t} (1 - k^u(i))
\]

\[
+ k^t(i)(n - w + 2w^t(i)) - w^t(i)
\]

\[
= \prod_{r=0}^{t} (1 - k^r(i)) + \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t} (1 - k^u(i))
\]

\[
+ k^t(i)(n - w + 2w^t(i)) - w^t(i)
\]

\[
= \prod_{r=0}^{t} (1 - k^r(i)) + \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t} (1 - k^u(i))
\]

\[
+ k^t(i)(n - w + 2w^t(i)) - w^t(i)
\]

\[
= \prod_{r=0}^{t} (1 - k^r(i)) + \sum_{r=0}^{t-1} \left( k^r(i)(n - w + 2w^r(i)) - w^r(i) \right) \prod_{u=r+1}^{t} (1 - k^u(i))
\]
This final equation completes the proof.

**Theorem 1.** If $K$ is secret, then after three iterations of $L_K$ the position of a bit of state is no longer related to its original position but depends only on fixed unknown data (as they are determined by $K$).

**Sketch of the proof.** We show that the term $\prod_{r=0}^{t-1}(1-k_{p^r(i)})$ on the right-hand side of the equation 2 vanishes after 3 iterations of $L_K$.

The positions $p^r(i)$ for $0 \leq r \leq t-1$ of bits of $K$ are not independent but the corresponding bits are independent since all bits of $K$ are drawn uniformly at random from $\{0,1\}$. Hence $1-k_{p^r(i)}$ for $0 \leq r \leq t-1$ can be considered as a random variable with equal probability of taking value 0 or 1. We know from [37] that when we draw uniformly at random $t$ bits, the longest streak of consecutive 1 we expect to have is $\Theta(\log_2 t)$. Therefore, for $t > 3$ there is necessarily some $u$ in the set of integer $\{0, \ldots, t - 1\}$ for which $1-k_{u(i)}$

### 5.1.3. Resistance to Algebraic Attacks

Algebraic attacks are known plaintext attacks. The adversary expresses the whole cipher as a system of multivariate algebraic equations and then tries to solve it using known plaintext-cipher text pairs in order to recover the secret key. SC is a 2-round cipher that uses a 4-bit to 4-bit S-box and operates on 64-bit block. Each-box can be described by 21 equations in 8 variables (4 inputs and 4 outputs). Therefore, SC can be expressed as a system of 672 multivariate equations in 256 variables. The number of equations is not impressive. However, the difficulty of using an algebraic attack against SC relies on the fact that it will not be easy (as theorem 1 implies) to bind the input variables of the S-boxes of the first round to the bits of the plaintext, to bind the output variables of the S-boxes of the first round to the input variables of the S-boxes of the second round and to bind the output variables of the S-boxes of the second round to the bits of the cipher text. Consequently, it is very unlikely that algebraic attack be effective against SC.

### 5.2. Security of RMAC

#### 5.2.1. Security of the Lightweight Key Establishment Protocol

Any modification on $\alpha$ will only change the way that $K_1$ and $K_2$ are extracted from $\beta$. A modification of $\alpha$ will also change the value of $\beta'$ (which is a one-time pad encryption of $\beta$) transmitted to the prover by the verifier. Since $\beta$ is drawn uniformly at random from $\{0,1\}^{2n}$, the attacker derives no benefit from its actions on $\alpha$.

#### 5.2.2. Security of the Core Authentication Protocol

The following theorem states that RMAC has the same resistance to MITM attacks as MM.

**Theorem 2.** If MM instantiated with an uf-rma MAC is a man-in-the-middle secure authentication protocol, and then RMAC instantiated with the same type of MAC is a man-in-the-middle secure authentication protocol.

**Proof.** For this proof, we use the reduction technique. That is from an instance of the MM protocol we simulate an instance of the RMAC protocol. And show that if there is a MITM adversary that has a non-negligible advantage on RMAC, it can be used to mount a MITM attack against MM with a non-negligible success probability.

Now, let $\mathcal{A}$ be a MITM probabilistic polynomial-time adversary attacking RMAC with a non-negligible success probability. We construct a MITM probabilistic polynomial-time adversary $\mathcal{A}'$ that attempts to attack MM. So, from an instance of the MM protocol, $\mathcal{A}'$ simulates for $\mathcal{A}$ an instance of RMAC as follows:
1. \( \mathcal{A}' \) begins by drawing uniformly at random \( \alpha \) from \( \{0,1\}^{2n} \) and sends it to \( \mathcal{A} \).
2. Upon receiving \( (r, \tau_3) \) from the MM verifier where \( \tau_3 = \text{TAG}_{K}(r) \), \( \mathcal{A}' \) draws uniformly at random \( r' \) from \( \{0,1\}^{n} \) and sends \( (r||r', \tau_3) \) to \( \mathcal{A} \). Since in the RMAC protocol \( \text{pfx}_n(\beta') \) is unrelated to \( \text{sfx}_n(\beta') \) and \( \beta' \) is obtained from a one-time pad of two unknown bit strings, the view of \( \mathcal{A} \) in this step is identically distributed to the view it has from the second step of RMAC.
3. \( \mathcal{A}' \) finishes the simulation by forwarding \( \tau_2 \) received from the MM prover to \( \mathcal{A} \), or if it doesn’t receive nothing, sends a uniformly and randomly selected \( n \)-bit string to \( \mathcal{A} \). Since the MAC is uf-rma, the adversary is not allowed to see MAC tags for chosen messages. Therefore, it will not be able to distinguish \( \text{TAG}_{K}(r) \) from \( \text{TAG}_{K}(r') \) for \( K \) and \( K' \) in \( \{0,1\}^{n} \). Thus, the view of \( \mathcal{A} \) in this step is identically distributed to the view it has from the final step of RMAC.

We claim that this simulation is correct since the view of \( \mathcal{A} \) when used as a sub-routine by \( \mathcal{A}' \) is identically distributed to the view it has when it interacts directly with RMAC. In conclusion, \( \mathcal{A} \) has the same advantage over RMAC as \( \mathcal{A}' \) has over MM (which is negligible [21]).

Encapsulating the challenge in \( \beta' \) using the one-time pad encryption reduces the security requirements on SC. Therefore, even if the attacker succeeded in finding a valid message-tag pair \((m, \tau)\), it has very little chance to reach the next step of the protocol since it will not know how to encapsulate \( m \) in \( \beta' \). Another aspect that reinforces the security of our protocol is that the prover returns a response to the verifier regardless the outcome of the verification \( (\text{pfx}_{n}(\beta'), \tau_3) \). This prevents the attacker from using the RMAC prover as a verification oracle since it has no way of detecting a change in the behaviour of the RMAC prover following the outcome of the verification of the pair \((\beta', \tau_3)\). This is a one more security element that our protocol RMAC has over the MM protocol. All this, allows us to say that our protocol can be seen as a generic construction (SC can be replaced by a uf-rma MAC) at least as secure as MM which is a man-in-the-middle secure authentication protocol.

6. CONCLUSIONS

In this paper, we have presented RMAC a new lightweight MAC authentication protocol for highly constrained IoT devices. RMAC consists of ultra-lightweight algorithms and takes advantage—but also adds some extra steps— of the design of MM, a two-round generic construction secure against man-in-the-middle attacks introduced by Mol et al. It also uses a new implementation of the extensively studied 2-round Xor-Cascade Encryption as a message authentication code. Although SC is not intended to be a block cipher for resource constrained devices, we have shown that it is resistant to linear or differential cryptanalysis or an algebraic attack. When viewed as a generic construction (SC replaced by an unforgettable under random-message attack MAC), RMAC is proven to be a secure MITM three rounds authentication protocol.

REFERENCES


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